

Module 9a – Inference Continued

[Review Against All Odds: Unit 26](#) (Inference)

Stat Procedure Diagram – Where we are

		<u>Descriptive Statistics (Describing Pops or Samples)</u>		<u>Inferential Statistics (from Samples)</u>
	Variable Types	Display	Describe	Estimation
Univariate	categorical (nominal or ordinal)*	Bar Graph/Pie Chart	Counts/Percentages	When binary/dichotomous: Confidence interval for proportions
	quantitative/continuous	Histogram/Stem & Leaf Box Plot	Mean/St Dev (normal) Median/Min, Q1, Q3, Max (skewed)	Confidence interval for means
		Display	Describe	Significance Tests/Hypothesis Tests
Bivariate	2 categorical	Tables or Bar Graphs	Two-way tables/Crosstabulation	Chi-square test (for goodness of fit)
	1 categorical, 1 quant.	Bar Graphs	Comparison of means/average	T-test (one sample/group, two samples/groups) ANOVA (two or more samples/groups)
	2 quant.	Scatterplot	Correlation Coef. (Coef. of determ)/ Regression Line	T-test for correlation
		Display	Describe	Significance Tests/Hypothesis Tests
Multivariate	Response Variable is Quant.	-	Ordinary Least Squares Regression (OLS)	F-test for overall model T-tests for each explanatory variable
	Response Variable is categorical (dichotomous)	-	Logistic Regression	Chi-square tests of significance

NOTE: Items highlighted in yellow are covered in this course.

*When a categorical variable has two categories, it is called dichotomous.

Still focused on...

...*confidence intervals* and *one sample z/t tests*

- Confidence Intervals (univariate)
- One sample z/t tests (bivariate)
- Do we know the population standard deviation?
 - If yes, we can use z in the formula
 - If no, we use t in the formula (in practice. this is what we typically use)

$$z = \frac{\bar{X} - \mu}{\sigma / \sqrt{n}} \quad \text{vs} \quad t = \frac{\bar{X} - \mu}{s / \sqrt{n}}$$

$$\bar{x} \pm z \frac{\sigma}{\sqrt{n}} \quad \text{vs} \quad \bar{x} \pm t \frac{s}{\sqrt{n}}$$

t-distribution vs z-distribution

[Watch Khan academy video](#)

(see course page for link)

Degrees of freedom DF

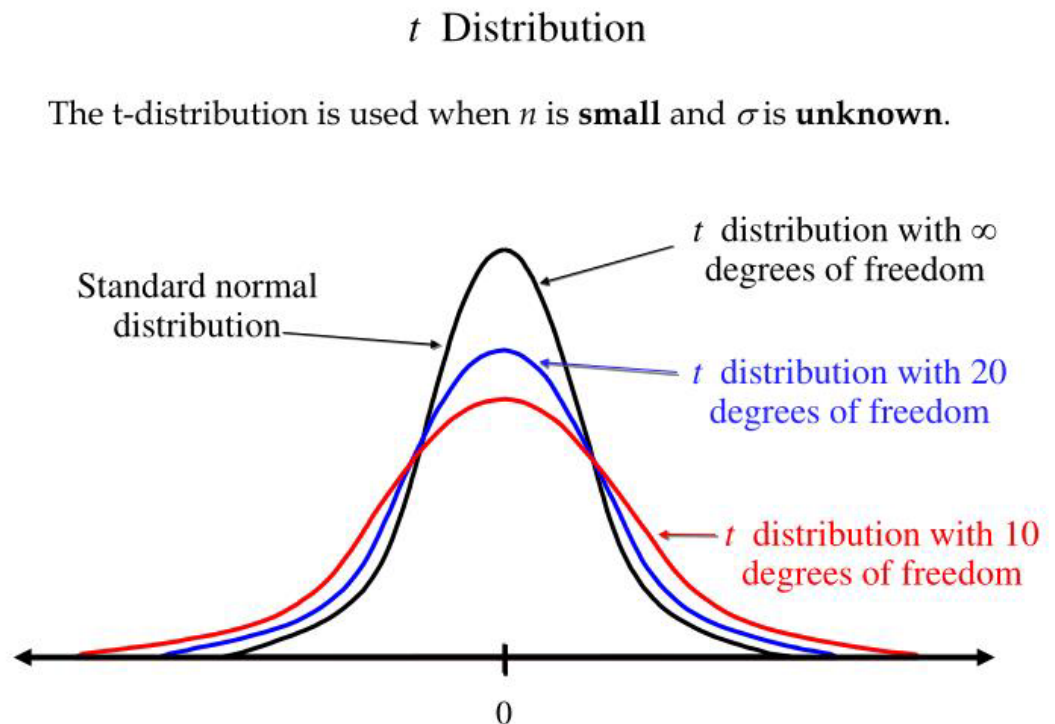
(for conf. intervals and
one-sample t-tests)=

$$\mathbf{n-1}$$

where n =sample size

**Smaller sample sizes
require more room for
error (wider tails).**

**The larger the sample
size, the closer we get to
a normal distribution**



t-distribution table (from page 701)

Confidence Intervals:
Row z: for confidence level
90%, 95%, 99%

Significance tests: One-
sided p and two-sided p
tells us the p-value that
corresponds with our z-
statistic

Table entry for C is the critical value t^* required for confidence level C.
To approximate one- and two-sided P-values, compare the value of the t statistic with the critical values of t^* that match the P-values given at the bottom of the table.

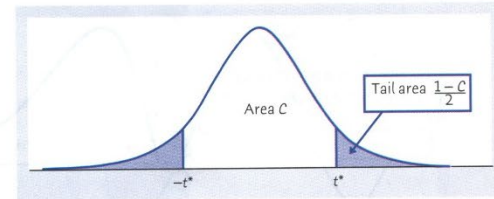


TABLE C t DISTRIBUTION CRITICAL VALUES


DEGREES OF FREEDOM	CONFIDENCE LEVEL C											
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92
4	0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	0.727	0.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	0.711	0.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408
8	0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5.041
9	0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587
11	0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015
17	0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22	0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
23	0.685	0.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	0.685	0.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
25	0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725
26	0.684	0.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707
27	0.684	0.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	0.683	0.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	0.683	0.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
30	0.683	0.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.646
40	0.681	0.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	0.679	0.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
60	0.679	0.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460
80	0.678	0.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	0.677	0.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
1000	0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
z*	0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
One-sided P	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
Two-sided P	.50	.40	.30	.20	.10	.05	.04	.02	.01	.005	.002	.001

Inference in practice – one sample t-test

- IV (Categorical) – Part of a group (yes/no)
- DV (Quantitative/Continuous)

- One sample
mean comparison:

- ***z-test***


$$Z = \frac{\bar{X} - \mu}{\sigma / \sqrt{n}}$$

μ =pop mean/some standard value

\bar{x} =sample mean

n =sample size

σ = population standard deviation